Space Shuttle Challenger

- January 28, 1986 - seal failure in a rocket booster causes the shuttle to explode, killing all seven astronauts.
- Three year investigation found technical and organizational issues.
- Became a case example studied in many forms of engineering.
Fault-Based Testing

By studying faults in previous designs, we can predict and prevent similar faults in future product designs.

Many testing techniques based on what we think should happen. We can also test based on knowledge of what has gone wrong before.
Used in Language Design

● Automated Garbage Collection
  ○ Prevents dangling pointers, memory leaks, other memory management faults.

● Automatic Array Bounds Checking
  ○ Does not prevent bad indexes from being used, but ensures they are noticed and limits damage.

● Type Checking
  ○ Prevents malformed values from being used as input or in computations.
Fault-Based Testing

- Model the type of faults we expect to see in a program.
  - Create alternate versions of the program with those faults.
  - Design tests that distinguish the real program from the faulty program.

- Process of fault seeding - deliberately creating programs with faults to see if our tests can find those intentional faults.
Uses of Fault Seeding

- **Fault seeding** can be used to:
  - Judge the adequacy of a test suite.
  - Select test cases to augment a suite.
  - Estimate the number of faults in a program.

- Provides evidence that we have done a good job in testing:
  - If our tests have not found any new faults, have they found all major issues, or are they bad tests?
  - Fault seeding helps answer this question.
    - Can the existing tests find the seeded faults?
Mutation Testing

- Encode common syntactic faults as *mutation operators*.
  - Functions that take in candidate program statements and insert the modeled fault.

- Produces a *mutant*.
  - A clone of the program with 1+ seeded faults.
Mutation Operators
Mutation Operators

- Intended to model common types of faults.
- Designed to be applied to any type of code, without human intervention.
- Tend to be simple syntactic faults.
  - Replacing one variable reference with another.
  - Changing a comparison from < to <=.
  - Referencing a parent class instead of a child.
Operand Modifications

- **X for Y replacement**
  - Replace constant \( C1 \) with constant \( C2 \).
  - Replace constant \( C \) with scalar variable \( S \).
  - Replace scalar \( S \) for constant \( C \).
  - Replace scalar \( S1 \) with scalar \( S2 \).
  - Replace scalar/constant with array reference \( A[I] \).
  - Replace array reference \( A[I] \) with scalar/constant.
  - Replace array reference with another array reference.
    - Either another array or another index in the same array.
Expression Modifications

● **Arithmetic Operators**
  ○ Binary operators: \( x (+, -, *, /, \% ) y \)
  ○ Unary operators: \(+x, -x\)
  ○ Shortcut operators: \(x++, ++x, x--, --x\)

● **Arithmetic Operator Replacement**
  ○ Replace binary/unary/shortcut operator with another.
  ○ Replace shortcut operator with a unary operator.

● **Arithmetic Operator Insertion**
  ○ Insert an additional operator into an expression.

● **Arithmetic Operator Deletion**
  ○ Remove an operator from an expression.
Expression Modifications

- **Conditional Operators**
  - Binary: $x$ $(\&\&, ||, \&, |, ^)$ $y$
  - Unary: $(~, !)x$

- **Relational Operators**
  - $x$ $(>,$ $\geq,$ $<,$ $\leq,$ $==,$ $!=$) $y$

- **Shift Operators**
  - $x$ $(\gg,$ $\ll,$ $\ggg)$ $y$

- **(Conditional/Relational/Shift) Operator Replacement, Insertion Deletion**
Expression Modifications

- **Shortcut Operators**
  - $x \ (+=, \ -=, \ *=, \ /=, \ %=, \ &=, \ |=, \ ^=, \ <<=, \ >>=) \ y$
  - Shortcut Operator Replacement

- **Absolute Value Insertion**
  - Replace a subexpression with $\text{abs}(e)$.

- **Constant for Predicate Replacement**
  - Replace a predicate $(a \ || \ b)$ with a constant truth value ($true/false$).
Statement Modifications

- **Statement Deletion**
  - Remove a random statement from the program.

- **Switch Case Replacement**
  - Replace the label of one case with another.

- **End Block Shift**
  - Move closing brackets to an earlier or later location.
Encapsulation/Inheritance Modifications

- **Access Modifier Change**
  - Change a modifier to *(public/protected/private)*

- **Hiding Variable Deletion**
  - Hiding variable - a variable in a subclass that has the same name and type as a variable in the parent.
  - Delete a hiding variable.
  - Causes references to that variable to access the version in the parent instead.

- **Hiding Variable Insertion**
  - Insert a hiding variable into a subclass.
  - Now, two variables of the same name exist.
Inheritance Modifications

- **Overriding Method Deletion**
  - Delete an overridden method from a subclass.
  - References call the version inherited from a parent.
- **Overridden Method Calling Position Change**
  - Overridden methods can call the parent method.
  - Moves calls to the parent version to other positions.
- **Super Keyword Insertion/Deletion**
  - Super keyword is used to access parent variables and methods within the child.
  - Inserts or deletes the keyword within methods.
Inheritance Modifications

- **Overridden Method Renamed**
  - Rename a method in the parent class that was overridden by the child.
  - Ensures that the overridden version is always called instead of the parent version.

- **Explicit Parent Constructor Call Deletion**
  - Deletes `super(parent)` constructor calls.
  - To kill, tests must cause and notice an incorrect initial state.
Polymorphism Modifications

- **New Method Call with Child Class Type**
  - Replace a declaration with a valid child instance.
    - `Parent a = new Parent();` becomes `Parent a = new Child();`

- **Variable/Parameter Declaration With Parent Class Type**
  - Change the declared type of a variable to its parent.
    - `Child a = new Child();` becomes `Parent a = new Child();`
    - `boolean equals(Child c){..}` becomes `boolean equals(Parent c){..}`
Polymorphism Modifications

● Type Case Operator Insertion/Deletion
  ○ Change the actual type of an object reference to the parent or child of the original type.
    ■ \( p\text{.toString()} \) becomes \((\text{Child} \ p).\text{toString()}\)
  ○ Or delete a type cast operator.

● Cast Type Change
  ○ \((\text{SomeChild} \ c).\text{toString()}\) becomes \((\text{OtherChild} \ c).\text{toString()}\)

● Reference Assignment with Other Compatible Type
  ○ Change an object reference to point to another compatible variable.
    ○ Object \( \text{obj} \);  
      \( \text{String s = “hello”;} \)
      \( \text{Integer i = new Integer(4);} \)
      \( \text{obj=s;} \)
  becomes
    ○ Object \( \text{obj} \);
      \( \text{String s = “hello”;} \)
      \( \text{Integer i = new Integer(4);} \)
      \( \text{obj=i;} \)
Polymorphism Modifications

- Overloading allows 2+ methods to have the same name if they have different signatures.
- Overloading Method Contents Change
  - Replace the body of a method with the body of another method with the same name.
- Overloading Method Deletion
  - Deletes one of the overloading methods.
- Argument of Overloading Method Change
  - Changes the order or number of arguments in an invocation, as long as there is a version that will accept the list.
Language-Specific Modifications

- Mutation operators can be written for a particular language.
- Java:
  - *this* insertion/deletion
  - Static modifier insertion/deletion
  - Member variable initialization deletion
  - Default constructor deletion
  - Getter/Setter method replacement
Mutation Testing
Mutation Testing

- Select *mutation operators* - code transformations that represent classes of faults that we are interested in.
- Generate *mutants* by applying mutation operators to the program.
- Execute the same tests against the program and mutants to *kill mutants*.
  - A mutant is killed if the test passes on the original program and fails on the mutant.
  - A mutant not killed is considered *live*. 
Mutation Testing

● Most mutation operators reflect small syntactic mistakes.
● Programmers do make such mistakes. However, many faults are actually conceptual mistakes.
  ○ Mistaken assumptions about requirements.
  ○ Forgotten requirements.
● Is mutation testing a viable technique?
Mutation testing is valid if seeded faults are representative of real faults.

**Competent Programmer Hypothesis**
- A faulty program differs from a correct program only by a small textual change.
- If so, we only have to distinguish the program from all such small variants.
- Assumption: the SUT is “close to” correct.
Coupling Effect

- Many faults are small syntactical errors.
- Conceptual faults often manifest as syntactical errors.
- Complex faults may result in larger textual differences.
  - However, mutation testing is still valid if test cases for simple issues can detect complex issues.
  - *Coupling Effect Hypothesis* - complex faults can be modeled as a set of small faults.
Coupling Effect

- A complex change to a program is a series of small changes.
- If one of these small changes is not masked by the effects of other changes, then a test case that can notice that change may also detect a more complex change.
- Mutation testing is effective if both the competent programmer hypothesis and coupling effect hypothesis hold.
Mutant Quality

To be used in testing, mutants must be:

● **Syntactically correct** (*valid*)
  ○ Mutants must compile and execute.

● **Plausible** (*useful*)
  ○ Must provide information on how the system works.

Can a mutant be valid, but not useful?
Mutant Quality

Mutants might remain live if:

● They are *equivalent* to the original program.
  ○ for(i=0; i < 10; i++)
  ○ for(i=0; i != 10; i++)
  ○ Identifying equivalency is NP-hard.

● Test suite is *inadequate* for that mutation.
  ○ (a <= b) and (a >= b) cannot be differentiated if a==b in the test case.
Mutation Coverage

Adequacy of the suite can be measured as:

\[
\frac{\text{(# mutants killed)}}{\text{(total mutants)}}
\]

- Mutants can be equivalent when both the original and the mutant are wrong.
- Helps ensure that the test suite is robust against the modeled mutation types.
Mutation and Structural Coverage

Mutation coverage can subsume structural coverage metrics.

- **Statement Coverage**
  - Apply statement deletion to all statements.
  - To kill a mutant where statement \( S \) has been deleted requires executing \( S \) in the original program.

- **Branch Coverage**
  - Apply constant replacement to all predicates.
  - To kill a mutant where a predicate is set to true, a test must execute the original with a false value.
Practical Considerations

Mutation testing is expensive.

- Must run *all* tests against *all* mutants.
- Many mutants typically generated.
  - One mutation operator applied per mutant.

- If cost is an issue, use “weak” mutation testing:
  - Apply multiple mutation operators per mutant.
Weak Mutation Testing

Mutation testing is expensive.

- Must run all tests against all mutants.
- Many mutants typically generated.
  - One mutation operator applied per mutant.

- If cost is an issue:
  - “weak” mutation testing - seed multiple faults per mutants.
  - Sample from space of mutants until statistical significance is achieved.
Weak Mutation Testing

- Seed multiple faults into a single mutant.
  - Called a “meta-mutant”
- Divide the program into segments and track internal state of both original and all mutants when executing a segment.
- Kill all detected mutants when intermediate state differs instead of waiting for output.
- Decreases the number of test executions.
A test suite that kills some mutants may be as effective at finding real faults as one that kills all mutants.

Mutation testing can be used to obtain a statistical estimate of the ability of the suite to detect mutations.

- Randomly generate $N$ mutants.
- Samples must be a valid statistical model of occurrence frequencies of real faults.
- Target 100% coverage over the sample.
## Estimating Number of Real Faults

- Mutants can be used to estimate the number of remaining faults in a program.

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<thead>
<tr>
<th>Number of Seeded Faults</th>
<th>Seeded Faults Detected</th>
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<tr>
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<tr>
<td>Number of Real Faults</td>
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<td>Real Faults Detected</td>
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### Be careful!

- We must have a reason to believe that our tests are as effective as real faults as seeded faults.
- Fault model must reflect the real program.
- These assumptions are rarely true.
1. How many mutations are possible for Relational Operator Replacement, Arithmetic Operator Replacement
2. Apply relational operator replacement operation to statement 4, design a test that would kill that mutant.
3. Design an equivalent mutant.
4. Design a valid, but useless mutant.
● How many mutations are possible:
  ○ Relational Operator Replacement:
    ■ for(int i=0; i < a.length; i++){
      ● (>=, <, <=, ==, !=), 5 mutations
    ■ if(a[i] < threshold){
      ● (>, >=, <=, ==, !=), 5 mutations
  ○ Arithmetic Operator Replacement
    ■ for(int i=0; i < a.length; i++){
      ● Shortcut replacement, (++i, i--, --i), 3 mutations
    ■ a[i]= -a[i];
      ● Unary replacement, (+a[i]), 1 mutation
      ● Unary to shortcut replacement, (a[i]++, ++a[i], a[i]--, --a[i]), 4 mutations
Activity - Solution

- Apply the relational operator replacement operation to statement 4:
  - if(a[i] < threshold) becomes:
    - if(a[i] == threshold)

- Design a test case that would kill that mutant.
  - a[-1,0,1]
    - -1 would not become positive.
Activity - Solution

- **Design an equivalent mutant.**
  - Can do so by applying the relational operator replacement operation to statement 4:
    - if(a[i] < threshold){ becomes:
      - if(a[i] <= threshold){
    - Since threshold=0, and -0 = 0, no test would detect this fault.
    - Does not help us test, as the fault cannot cause a failure.
Design a valid, but useless mutant.

- For example: mutant that compiles, but trivially fails.
- Apply the relational operator replacement operation to statement 4:
  - if(a[i] < threshold) becomes:
  - if(a[i] > threshold)
  - Any positive numbers are made negative, all negative remain negative. Almost any test would detect this.
- Many mutants are useless for detecting real faults.
We Have Learned

● Mutation testing is the process of inserting faults to help develop a test suite that can detect unknown real faults.

● Mutation operators automatically create faulty versions of a program.
  ○ Operators model expected fault types.

● Tests are judged according to their ability to detect faults.
Next Time

● **Midterm Review**
  ○ Practice Midterm on Dropbox site. Try it out!
  ○ Answers will be revealed after the review

● **Homework:**
  ○ Homework 2 - questions?