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# Lecture 9: Test Adequacy and Structural Testing

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# We Will Cover

- Test Adequacy Criteria
- Structural Testing:
  - Use structural coverage to judge tests, create new tests.
  - Statement, Branch, Condition, Path Coverage

**Every developer must answer:  
Are our tests are any good?**

**More importantly... Are they good  
enough to stop writing new tests?**

# Have We Done a Good Job?

What we want:

- We've found all the faults.

What we (usually) get:

- We compiled and it worked.
- We run out of time or budget.
  - **(Inadequate testing).**

## November 2020

| Sunday | Monday | Tuesday | Wednesday | Thursday | Friday | Saturday |
|--------|--------|---------|-----------|----------|--------|----------|
| 1      | 2      | 3       | 4         | 5        | 6      | 7        |
| 8      | 9      | 10      | 11        | 12       | 13     | 14       |
| 15     | 16     | 17      | 18        | 19       | 20     | 21       |
| 22     | 23     | 24      | 25        |          |        |          |
| 29     | 30     |         |           |          |        |          |



# Test Adequacy Criteria

Can we **compromise between the impossible and the inadequate?**



- Measure “good testing”
- **Test adequacy criteria** “score” tests by measuring completion of **test obligations**.
  - Checklists of properties that must be met by test cases.

# (In)Adequacy Criteria

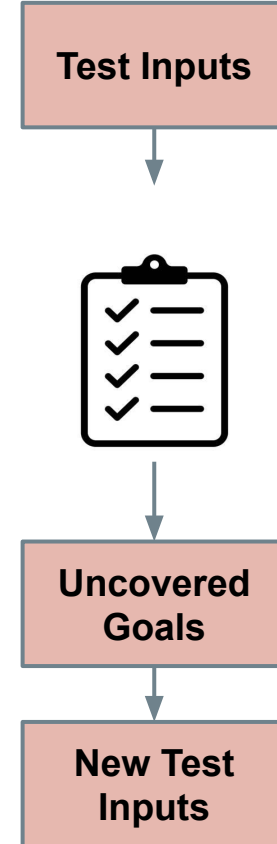
- Criteria identify **inadequacies** in the tests.
  - If no test reaches a statement, test suite is inadequate for finding faults in that statement.
  - If we plant a fake fault and no test exposes it, our tests are inadequate at detecting that fault.
- Tests may still miss faults, but maximizing criteria shows that tests *at least* meet certain goals.

# Adequacy Criteria

- Adequacy Criteria based on coverage of factors correlated to finding faults (*hopefully*).
  - Exercising elements of source code (**structural testing**).
  - Detection of planted faults (**mutation testing**)
- Widely used in industry - easy to understand, cheap to calculate, offer a checklist.
  - Enable tracking of “testing completion”
  - Can be measured in IntelliJ, Eclipse, etc.

# Use of Criteria

- Measure adequacy of existing tests
  - Create additional tests to cover missed obligations.
- Create tests directly
  - Choose specific obligations, create tests to cover those.
  - Targets for automated test generation.





# Structural Testing

# Structural Testing

- The structure of software is valuable information.
- Prescribe how code elements should be executed, and measure coverage of execution.
  - If-statements, Boolean expressions, loops, switches, paths between statements...

```
int[] flipSome(int[] A, int N, int X)
{
    int i=0;
    while (i<N and A[i] <X)
    {
        if (A[i] < 0)
            A[i] = - A[i];
        i++;
    }
    return A;
}
```

**The basic idea:  
You can't find all of the  
faults without exercising all  
of the code.**

# Structural Testing - Motivation

- Requirements-based tests should execute *most* code, but will rarely execute all of it.
  - Helper functions.
  - Error-handling code.
  - Requirements missing outcomes.
- Structural testing compliments functional testing by covering gaps in the source code.

# Structural Does Not Replace Functional

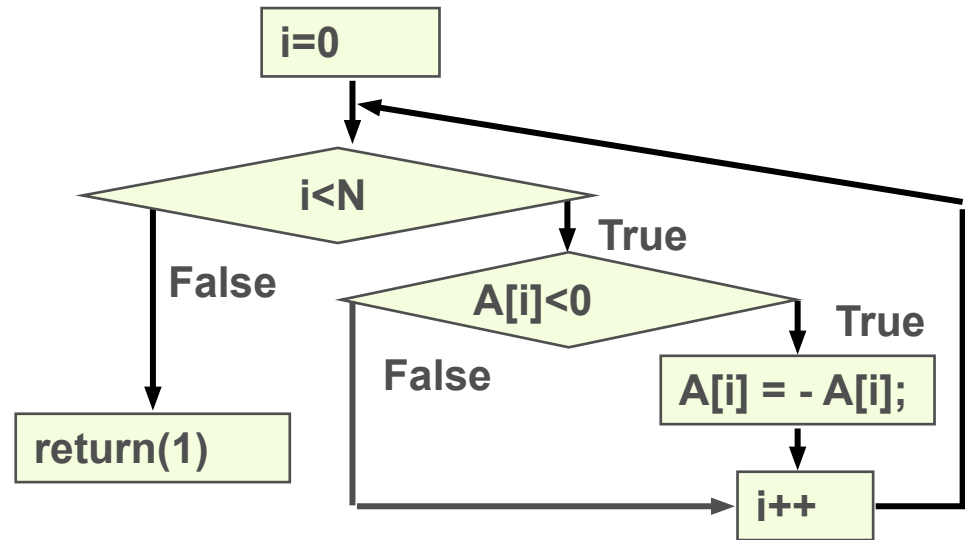
- **Should not be the basis for all test cases!!!!**
- Harder to make verification argument.
  - May not map directly to requirements.
- Does not expose missing functionality.
- Useful for supplementing functional tests.
  - Functional tests good at exposing *conceptual faults*.
  - Structural tests good at exposing *coding mistakes*.

# Control and Data Flow

- We need to understand how system executes.
  - Conditional statements result in branches in execution, jumping between blocks of code.
- **Control flow**: how control passes through code.
  - Which code is executed, and when.
- **Data flow**: how data passes through code.
  - How variables are used in different expressions.

# Control-Flow Graphs

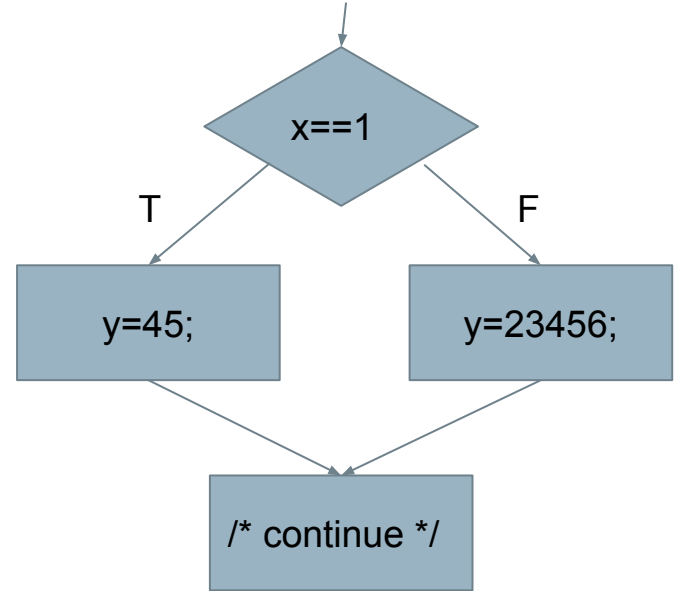
- Directed graph representing flow of control.
- Nodes represent blocks of sequential statements.
- Edges connect nodes in the sequence they are executed.
  - Multiple edges indicate conditional statements.



# Control Flow: If-then-else

```

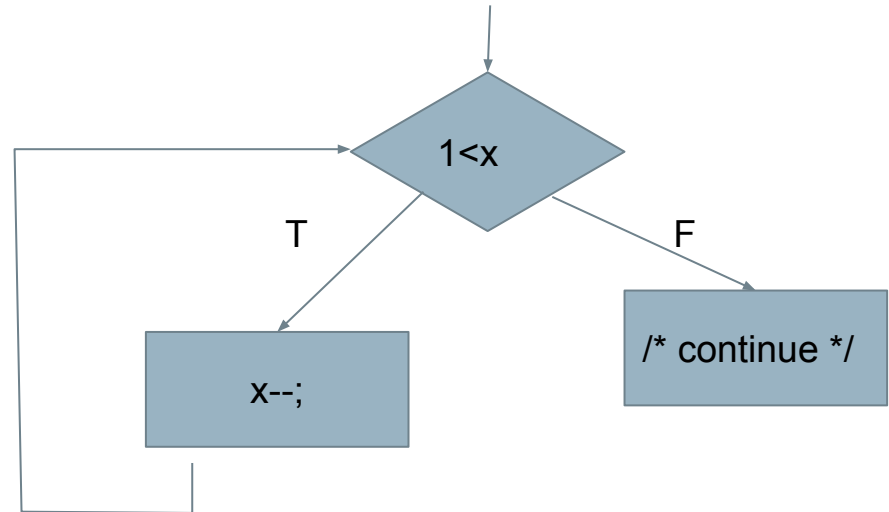
1  if (x==1) {
2      y=45;
3  } else {
4      y=23456;
5  }
6  /* continue */
  
```





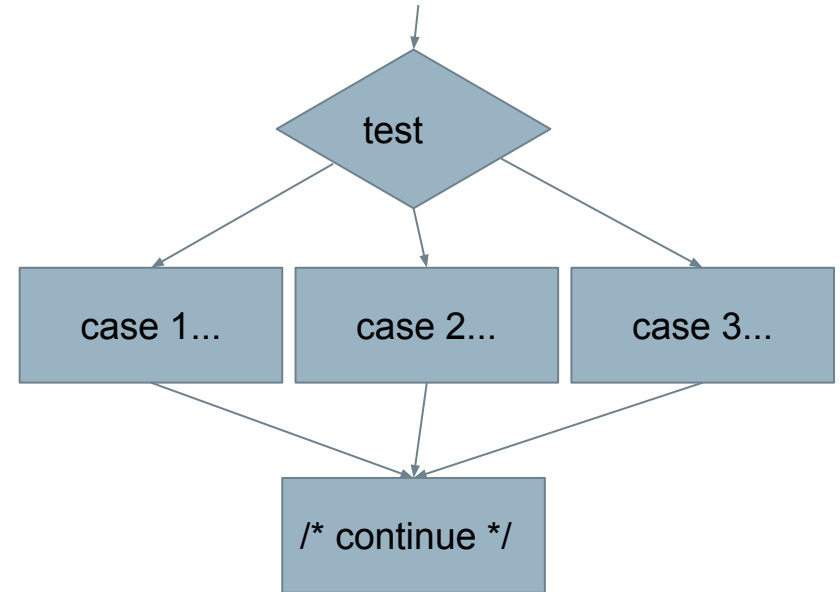
# Loop

```
1  while (1<x) {  
2      x--;  
3  }  
4  /* continue */
```



# Case

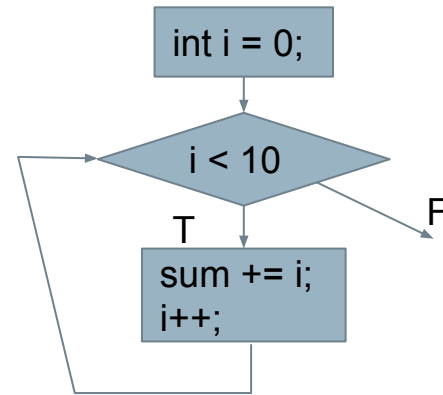
```
1  switch (test) {  
2      case 1 : ...  
3      case 2 : ...  
4      case 3 : ...  
5  }  
6  /* continue */
```



# Basic Blocks

- Nodes are basic blocks.
  - Sequential instructions with one entry and exit.
- Typically adjacent statements
  - One line might be broken up (e.g., loop setup is really three statements).

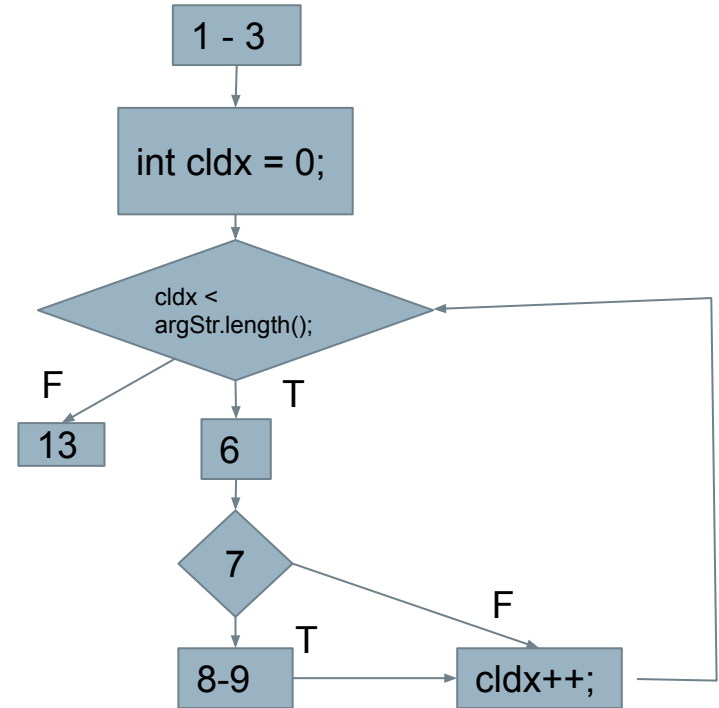
```
for(int i=0; i < 10; i++){  
    sum += i;  
}
```



# Control Flow Graph Example

```

1. public static String collapseNewlines(String argSt){
2.     char last = argStr.charAt(0);
3.     StringBuffer argBuf = new StringBuffer();
4.
5.     for(int cldx = 0; cldx < argStr.length(); cldx++){
6.         char ch = argStr.charAt(cldx);
7.         if (ch != '\n' || last != '\n'){
8.             argBuf.append(ch);
9.             last = ch;
10.        }
11.    }
12.
13.    return argBuf.toString();
14. }
  
```



# Structural Coverage Criteria

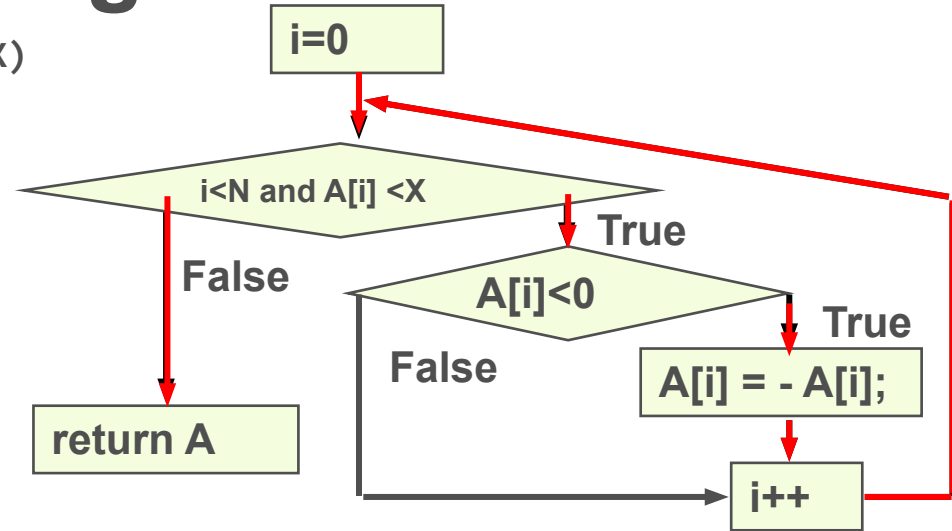
- Criteria based on exercising:
  - Statements (nodes of CFG)
  - Branches (edges of CFG)
  - Conditions
  - Paths
  - ... and many more
- Measurements used as adequacy criteria

# Statement Coverage

- Most intuitive criteria. Did we execute every statement at least once?
  - *Cover each node of the CFG.*
- The idea: a fault in a statement cannot be revealed unless we execute the statement.
- Coverage = 
$$\frac{\text{Number of Statements Covered}}{\text{Number of Total Statements}}$$

# Statement Coverage

```
int[] flipSome(int[] A, int N, int X)
{
    int i=0;
    while (i<N and A[i] <X)
    {
        if (A[i] < 0)
            A[i] = - A[i];
        i++;
    }
    return A;
}
```



Can cover in one test: [-1], 1, 10

# A Note on Test Suite Size

- Coverage not correlated to test suite size.
  - Some tests might not cover new code.
- However, larger suites often find more faults.
  - They exercise the code more thoroughly.
  - **How** code is executed often more important than **whether** it was executed.



# Test Suite Size

- **Design small targeted tests**, not long tests.
  - If test targets few obligations, it is easier to debug.
  - If a test covers many obligations, harder to understand the purpose, harder to locate and fix faults.
  - Exception - if cost to execute each test is high.

# Branch Coverage

- Do tests execute all outcomes of control-diverging statements (loop, if, switch)?
  - Cover each edge of the CFG.
- Helps identify faults in decision statements.
- Coverage = 
$$\frac{\text{Number of Branches Covered}}{\text{Number of Total Branches}}$$

# Subsumption

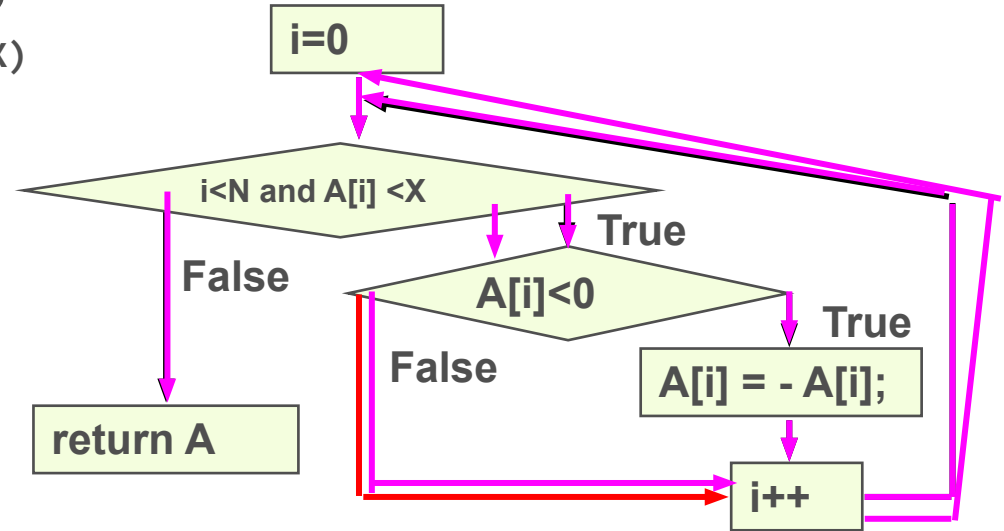
- Criterion A **subsumes** Criterion B if, for every program  $P$ , every test suite satisfying A also satisfies B on  $P$ .
  - *If we satisfy A, we have satisfied B.*
- Branch coverage **subsumes** statement coverage.
  - Covering all edges in CFG requires covering all nodes.

# Subsumption

- Shouldn't we always choose the stronger metric?
- Not always...
  - Typically requires **more** obligations.
    - (so, you have to come up with more tests)
  - Or **tougher** obligations.
    - (making it harder to come up with the tests).
  - May end up with **unsatisfiable** obligations.
    - (no test can cover these obligations)

# Branch Coverage

```
int[] flipSome(int[] A, int N, int X)
{
    int i=0;
    while (i<N and A[i] <X)
    {
        if (A[i] < 0)
            A[i] = - A[i];
        i++;
    }
    return A;
}
```



- $([-1], 1, 10)$  leaves one edge uncovered.
- $([-1, 1], 2, 10)$  achieves Branch Coverage.

**Let's take a break.**

# Decisions and Conditions

- A *decision* is a Boolean expression.
  - Often part of control-flow branching:
    - `if ((a && b) || !c) { ...`
  - But not always:
    - `Boolean x = ((a && b) || !c);`

# Decisions and Conditions

- A **decision** is a Boolean expression.
  - Made up of **conditions**
    - Connected with Boolean operators (and, or, xor, not):
    - Boolean variables: `Boolean b = false;`
    - Subexpressions that evaluate to true/false involving (<, >, <=, >=, ==, and !=): `Boolean x = (y < 12);`



# Decision Coverage

- Branch Coverage covers a *subset* of decisions.
  - Branching decisions that decide how control is routed through the program.
- Decision coverage requires that ***all*** decisions evaluate to all outcomes.
- Coverage = 
$$\frac{\text{Number of Decisions Covered}}{\text{Number of Total Decisions}}$$

# Basic Condition Coverage

- Several coverage metrics examine the *individual conditions* that make up a *decision*.
- Identify faults in decision statements.

(**a == 1** || b == -1) instead of (a == -1 || b == -1)

- Most basic form: make each condition T/F.
- Coverage = 
$$\frac{\text{Number of Truth Values for All Conditions}}{2x \text{ Number of Conditions}}$$

# Basic Condition Coverage

- Make each condition both True and False

**(A and B)**

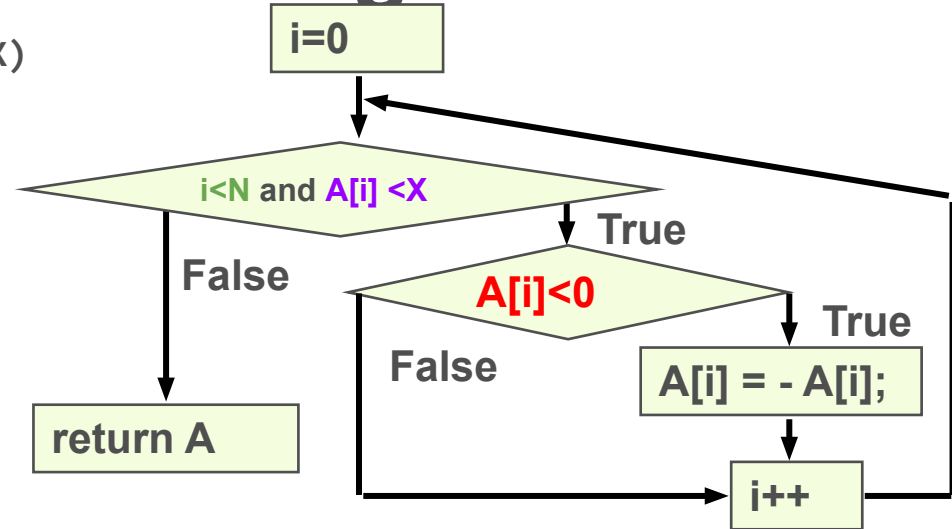
| Test Case | A     | B     |
|-----------|-------|-------|
| 1         | True  | False |
| 2         | False | True  |

- Does not require covering both outcomes.
  - Does not subsume branch or decision coverage.
  - (In this case, false outcome for both tests)

# Basic Condition Coverage

```

int[] flipSome(int[] A, int N, int X)
{
    int i=0;
    while (i<N and A[i] <X)
    {
        if (A[i] < 0)
            A[i] = - A[i];
        i++;
    }
    return A;
}
  
```



- $([-1, 1], 2, 10)$ 
  - Negative value in array
  - Positive value (but  $< X$ )
- $([11], 1, 10)$ 
  - Positive, but  $> X$
- Both eventually cause  $i < N$  to be false.

# Compound Condition Coverage

- Evaluate every combination of the conditions

(A and B)

| Test Case | A     | B     |
|-----------|-------|-------|
| 1         | True  | True  |
| 2         | True  | False |
| 3         | False | True  |
| 4         | False | False |

- Subsumes branch and decision coverage.
  - All outcomes are now tried.
- Can be **expensive** in practice.

# Compound Condition Coverage

- Requires **many** test cases.

(A and  
(B and  
(C and  
D))))))

| Test Case | A     | B     | C     | D     |
|-----------|-------|-------|-------|-------|
| 1         | True  | True  | True  | True  |
| 2         | True  | True  | True  | False |
| 3         | True  | True  | False | True  |
| 4         | True  | True  | False | False |
| 5         | True  | False | True  | True  |
| 6         | True  | False | True  | False |
| 7         | True  | False | False | True  |
| 8         | True  | False | False | False |
| 9         | False | True  | True  | True  |
| 10        | False | True  | True  | False |
| 11        | False | True  | False | True  |
| 12        | False | True  | False | False |
| 13        | False | False | True  | True  |
| 14        | False | False | True  | False |
| 15        | False | False | False | True  |
| 16        | False | False | False | False |

# Short-Circuit Evaluation

- In many languages, if the first condition determines the result of the entire decision, then fewer tests are required.
  - If A is false, B is never evaluated.

**(A and B)**

| Test Case | A     | B     |
|-----------|-------|-------|
| 1         | True  | True  |
| 2         | True  | False |
| 3         | False | -     |

# Modified Condition/Decision Coverage(MC/DC)

- Requires:
  - Each **condition** evaluates to true/false
  - Each **decision** evaluates to true/false
  - Each condition shown to **independently affect outcome** of each decision it appears in.

| Test Case | A                | B                | (A and B)        |
|-----------|------------------|------------------|------------------|
| 1         | True             | True             | True             |
| 2         | True             | False            | False            |
| 3         | False            | True             | False            |
| 4         | <del>False</del> | <del>False</del> | <del>False</del> |

- Tests 1, 3 show independent impact of A.
- Tests 1, 2 show independent impact of B.
- Test 4 adds nothing and can be skipped.



# Activity

Draw the CFG and write tests that provide statement, branch, and basic condition coverage over the following code:

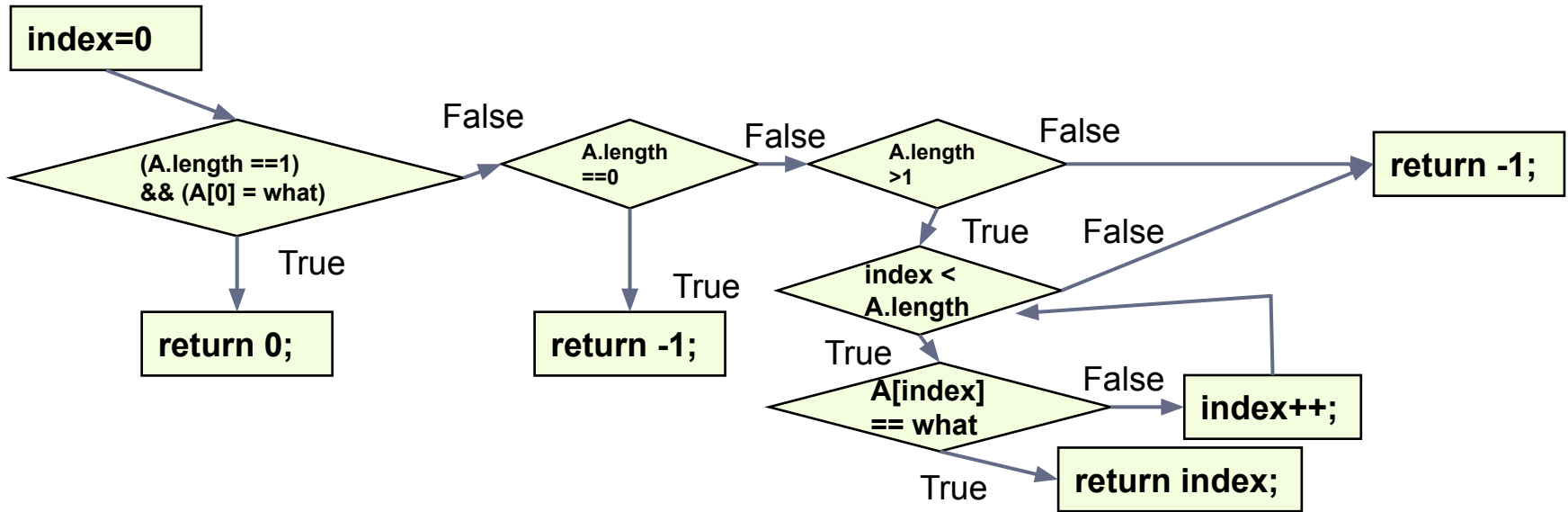
```
public int search(String[] A, String what){
    int index = 0;
    if ((A.length == 1) && (A[0] == what)){
        return 0;
    } else if (A.length == 0){
        return -1;
    } else if (A.length > 1){
        while(index < A.length){
            if (A[index] == what){
                return index;
            } else
                index++;
        }
    }
    return -1;
}
```

**[ ] (empty array), "Bob"**

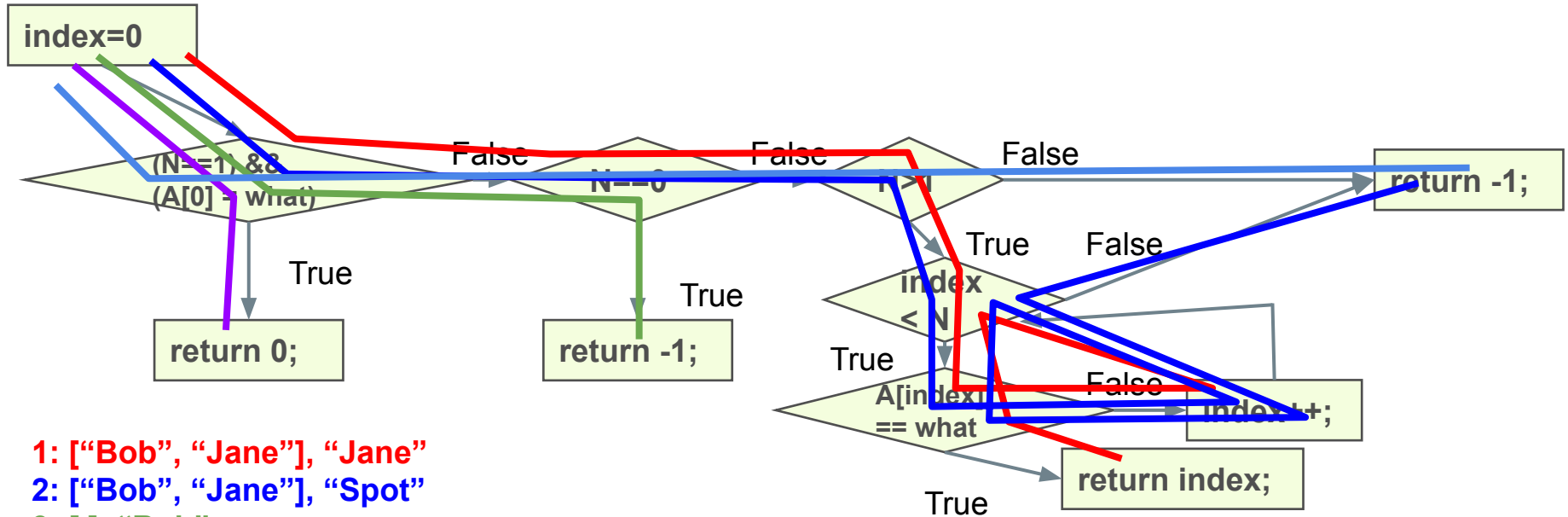
**Executes lines:**

**1, 2, 3,  
(Branch 3-F),  
5,  
(Branch 5-T),  
6**

# Activity - Control Flow Graph



# Activity - Possible Solution



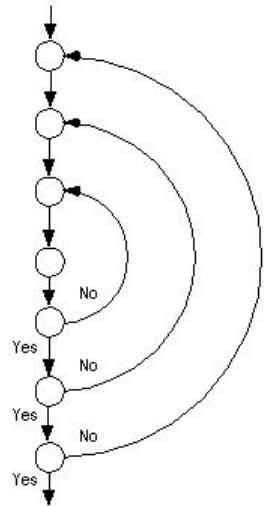
- 1: ["Bob", "Jane"], "Jane"
- 2: ["Bob", "Jane"], "Spot"
- 3: [], "Bob"
- 4: ["Bob"], "Bob"
- 5: ["Bob"], "Spot"

# Loop Boundary Coverage

- Focus on problems related to loops.
- For each loop, write tests that:
  - Skip the loop entirely.
  - Take exactly one pass through the loop.
  - Take two or more passes through the loop.

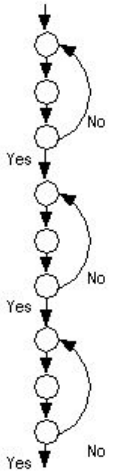
# Nested Loops

- Often, loops are nested within other loops.
  - For each level, execute 0, 1, 2+ times
- In addition:
  - Test innermost loop first with outer loops executed minimum number of times.
  - Move one loops out, keep the inner loop at “typical” iteration numbers, and test this layer as you did the previous layer.
  - Continue until the outermost loop tested.



# Concatenated Loops

- One loop executes. Next line of code starts a new loop. These are generally independent.
- If not, follow a similar strategy to nested loops.
  - Start with bottom loop, hold higher loops at minimal iterations
  - Work up towards the top, holding lower loops at “typical” iteration numbers.



# Why These Loop Strategies?

- If proving correctness, we establish preconditions, postconditions, and invariants that are true on each execution of loop.
  - The loop executes zero times when the postconditions are true in advance.
  - The loop invariant is true on loop entry (one), then each loop iteration maintains the invariant (many).
    - (invariant and !(loop condition) implies postconditions are met)
- Loop testing strategies echo these cases.

# Activity: Binary Search

For the binary-search code:

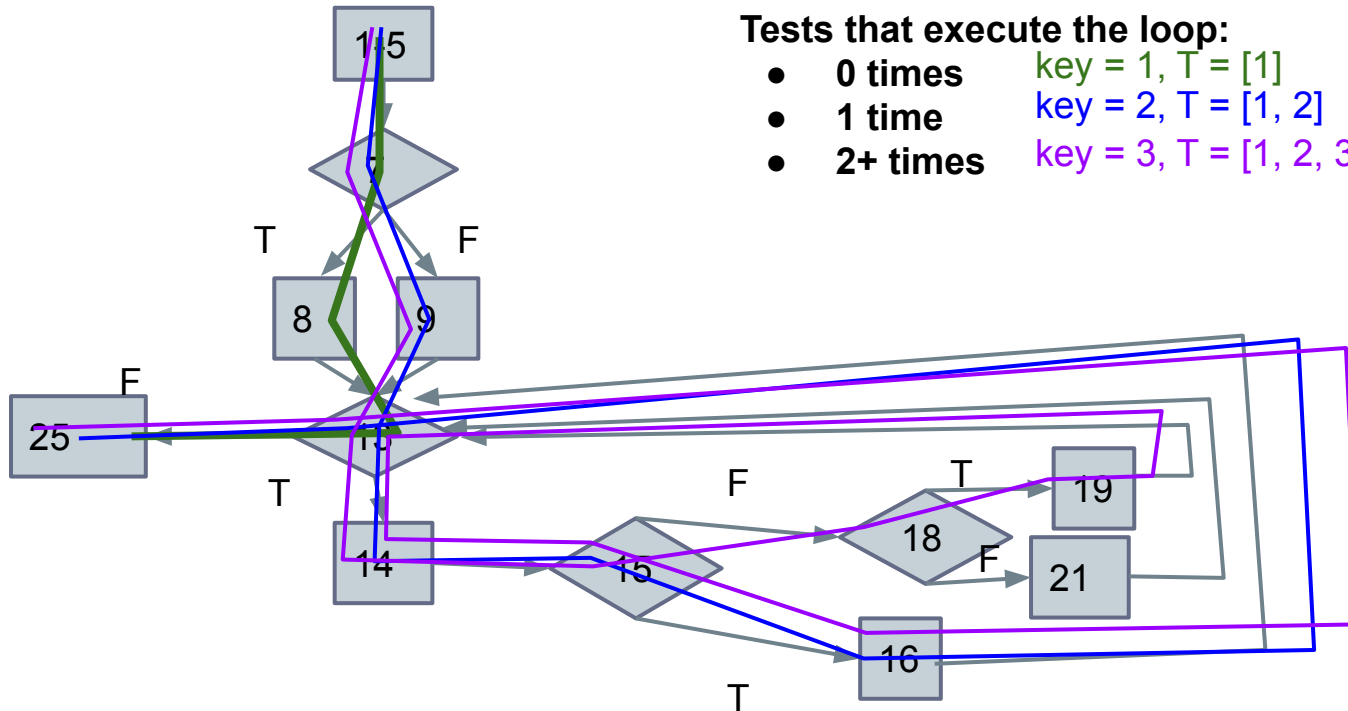
1. Draw the control-flow graph for the method.
2. Develop a test suite that achieves loop boundary coverage (executes while loop 0, 1, 2+ times).



# Activity: Binary Search

Tests that execute the loop:

- 0 times     $\text{key} = 1, T = [1]$
- 1 time     $\text{key} = 2, T = [1, 2]$
- 2+ times     $\text{key} = 3, T = [1, 2, 3]$



# The Infeasibility Problem

**Sometimes, no test can satisfy an obligation.**

- Impossible combinations of conditions.
- Error-handling for problems that can't really occur.
- Dead code.

# The Infeasibility Problem

- Stronger criteria call for potentially infeasible combinations of elements.

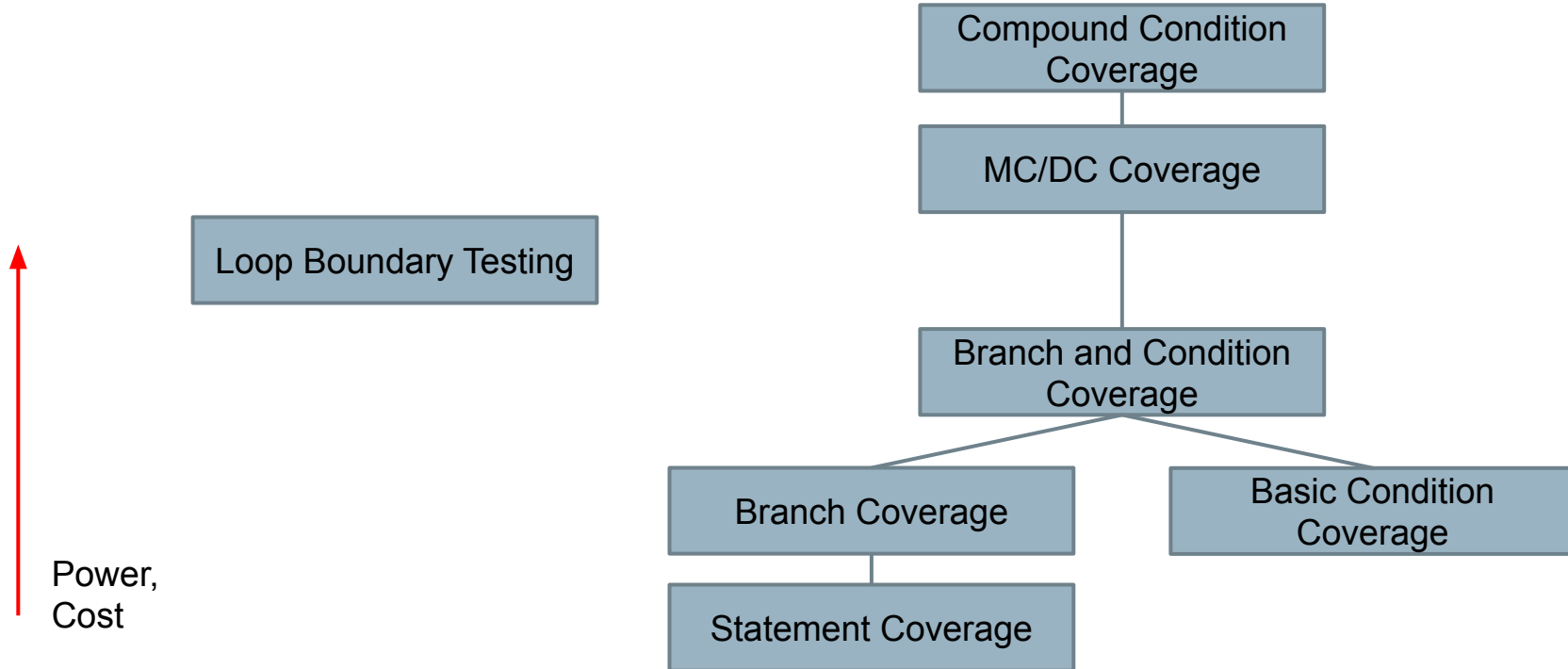
$$(a > 0 \ \&\& \ a < 10)$$

- It is not possible for both conditions to be false.
  - A would negative and greater than 10
- Loop boundary coverage
  - Maybe a loop can't be skipped.

# The Infeasibility Problem

- Adequacy “scores” based on coverage.
  - 95% branch coverage, 80% MC/DC coverage, etc.
  - Stop once a threshold is reached.
  - Unsatisfactory - obligations are not equally important.
- Manual justification for omitting each impossible test obligation.
  - Helps refine code and testing efforts.
  - ... but very time-consuming.

# Which Coverage Criterion Should I Use?



# We Have Learned

- Test adequacy “measures” how good our tests are.
  - Covering obligations removes inadequacies from suites.
- Code structure is used in many adequacy criteria.
  - Based on statements, branches, conditions, loops, etc.

# Next Time

- Next class: Path-based coverage and data-flow
- Thursday Exercise Session: Structural Coverage
- Homework - Assignment 2 due Feb 25



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